UNIVERSITY^{OF} BIRMINGHAM University of Birmingham Research at Birmingham

Epilepsy surgery: Evaluating robustness using dynamic network models

Junges, Leandro; Woldman, Wessel; Benjamin, Oscar; Terry, John

Citation for published version (Harvard): Junges, L, Woldman, W, Benjamin, O & Terry, J 2020, 'Epilepsy surgery: Evaluating robustness using dynamic network models', *Chaos*, vol. 30, no. 113106.

Link to publication on Research at Birmingham portal

General rights

Unless a licence is specified above, all rights (including copyright and moral rights) in this document are retained by the authors and/or the copyright holders. The express permission of the copyright holder must be obtained for any use of this material other than for purposes permitted by law.

•Users may freely distribute the URL that is used to identify this publication.

•Users may download and/or print one copy of the publication from the University of Birmingham research portal for the purpose of private study or non-commercial research.

•User may use extracts from the document in line with the concept of 'fair dealing' under the Copyright, Designs and Patents Act 1988 (?) •Users may not further distribute the material nor use it for the purposes of commercial gain.

Where a licence is displayed above, please note the terms and conditions of the licence govern your use of this document.

When citing, please reference the published version.

Take down policy

While the University of Birmingham exercises care and attention in making items available there are rare occasions when an item has been uploaded in error or has been deemed to be commercially or otherwise sensitive.

If you believe that this is the case for this document, please contact UBIRA@lists.bham.ac.uk providing details and we will remove access to the work immediately and investigate.

1 2

3

4 5

Epilepsy Surgery: Evaluating robustness using dynamic network models

Leandro Junges^{1,2,*,a}, Wessel Woldman^{1,2,*}, Oscar J. Benjamin³, John R. Terry^{1,2}

6 Affiliations 7

8 ¹ Centre for Systems Modelling and Quantitative Biomedicine, University of Birmingham,

9 Birmingham, B15 2TT, United Kingdom.

² Institute for Metabolism and Systems Research, University of Birmingham, Birmingham, B15 2TT,
 United Kingdom.

- ³ Department of Engineering Mathematics, University of Bristol, Bristol, BS8 1UB United Kingdom.
- 13 * Denotes equal contribution as first author.
- 14 ^a Corresponding author: l.junges@bham.ac.uk.
- 15

16

17 Abstract

18

Epilepsy is one of the most common neurological conditions, affecting over 65 million people 19 worldwide. Over one third of people with epilepsy are considered refractory: they do not respond to 20 drug treatment. For this significant cohort of people, surgery is a potentially transformative treatment. 21 However, only a small minority of people with refractory epilepsy are considered suitable for surgery 22 23 and long-term seizure freedom is only achieved in one half of cases. Recently, several computational 24 approaches have been proposed to support presurgical planning. Typically, these approaches use a 25 dynamic network model to explore the potential impact of a surgical resection in silico. The network component of the model is informed by clinical imaging data and is considered static thereafter. This 26 27 assumption critically overlooks the plasticity of the brain and therefore how continued evolution of the brain network post-surgery may impact upon the success of a resection in the longer term. In this 28 work, we use a simplified dynamic network model, that describes transitions to seizures, to 29 30 systematically explore how network structure influences seizure propensity, both before and after virtual resections. We illustrate key results in small networks, before extending our findings to larger 31 32 networks. We demonstrate how evolution of brain networks post resection can result in a return to increased seizure propensity. Our results effectively determine the robustness of a given resection to 33 network reconfiguration and so provide a potential strategy for optimising long-term seizure freedom. 34

35 36

37 Brain surgery is a potentially life-changing treatment for people with epilepsy that do not respond to drug therapy. Unfortunately, identifying brain regions responsible for seizure 38 39 generation and spread is complex and so the number of people considered suitable for surgery 40 is relatively low and outcomes are non-optimal. Many people for whom surgery appears initially successful see seizures return within a year or so. Several computational methods that combine 41 network analysis and mathematical modelling have been proposed lately to support surgical 42 planning by evaluating virtually the potential impacts of a surgical resection. In such models, 43 representations of brain networks are extracted from clinical data. However, these methods 44 typically consider brain networks to be static after surgery, ignoring the potential effects of 45 network reorganization in long-term seizure freedom. In this work we use a dynamic network 46 model of seizure transition to systematically evaluate the influence of network structure in 47 seizure propensity before and after virtual resections. We use small networks to illustrate how a 48 49 successful resection can be adversely influenced by post-surgical network reconfiguration, where the creation or destruction of network edges lead to an increase in seizure propensity. We then 50

extend our results to networks with sizes more in line with what is typically obtained from clinical data. The results presented in this work shed light upon the issue of brain networks sensitivity to reconfiguration, and provide a framework to evaluate the robustness of therapeutic interventions. This framework can potentially be used more generally to explore robustness in the behaviour of dynamic coupled systems.

56 57

59

58 I. Introduction

Epilepsy is a very common serious primary neurological condition¹. Epilepsy is characterised by the 60 tendency to have spontaneous seizures². In some cases, the cause of seizures is readily apparent (e.g. 61 a brain tumour or cortical lesion), however for the majority the definitive cause is unknown. With 62 63 appropriate treatment, approaching two-thirds of people with epilepsy have well-controlled seizures³. For the remaining third, more invasive therapies including electrical stimulation⁴ and surgery⁵ are 64 potential options. For those people with epilepsy for whom surgery is considered appropriate, long-65 term seizure freedom is achieved in around 50% of cases. However, success rates may be as high as 66 67 80% where an affected brain region is clearly identifiable, but as low as 15% in cases where no such brain region is apparent⁶. A further consideration is the lasting impact of the surgery. 68 Many people with epilepsy display a reduction in seizure rates immediately after surgery, however 69 70 their seizures often return over time and may be different in nature to those with which they were initially diagnosed^{6,7}. Despite these challenges, epilepsy surgery has been shown to be a highly cost-71 effective solution⁸ and many believe it should gain more widespread acceptance as an alternative 72 treatment for people with refractory epilepsy^{9,10}. 73

74

75 One explanation for this wide variation in surgery success rates is the role of large-scale brain 76 networks in seizure generation, which has become increasingly recognised in recent years^{11–16}. This 77 recognition has resulted in the International League Against Epilepsy updating its operational classification of seizure types to reflect the role networks play in the generation of 78 79 seizures¹⁷. Clinically, brain networks can be characterised through structural or functional relationships. Structural connections essentially represent the anatomical links between brain regions 80 as typically measured using magnetic resonance imaging (MRI). These structural links are 81 hypothesised to form the basis of functional connections between brain areas. Typically, functional 82 inferred statistically from time-series data such as functional 83 connections are MRI. electroencephalography (EEG), or magnetoencephalography (MEG) (see Stam¹⁸ for a comprehensive 84 85 review).

86

However, as van Mierlo and colleagues observed¹⁶: "With the growing enthusiasm for connectivity it 87 is often overlooked that in reality, all we have are statistical interdependencies of signals, which 88 89 should be interpreted cautiously." Because of the largely qualitative nature of these clinically defined 90 networks, there has been considerable interest in the development and application of mathematical methods, notably from network science and dynamical systems, to better understand seizure 91 generation and therefore the condition of epilepsy¹⁹. For example, in early work²⁰ a dynamic network 92 model was constructed to demonstrate that emergent activity characteristic of different seizures 93 types could arise due to changes in either the edge structure of the network, or the dynamic activity 94 95 within nodes. The dynamics within each node of this model are determined by a bistable switch that 96 characterises transitions between phenomenological representations of healthy (background) and pathological (seizure) states. Based upon the normal form of a sub-critical Hopf bifurcation, this class 97 of model was first introduced in the context of epilepsy by Kalitzin *et al.*²¹ and Benjamin *et al.*²². 98 99 Although a gross simplification of the brain, the model provided insight as to why loss of connections between brain regions made the brain – on average – more seizure prone. Many subsequent approaches 100

have since built on this concept of seizures as an emergent property of the interplay between nodes within a network and its connectivity (see Milton²³ for a classical introduction and Moraes *et al.*²⁴ for a recent review).

104

105 A number of approaches have recently been developed that combine clinical data with mathematical models to understand surgical strategies or to inform pre-surgical planning. For example, a 106 107 computational study²⁵ identified differences between structural brain networks of people with temporal lobe epilepsies and healthy controls. They further showed that measures of seizure rates (as 108 calculated model) could be lowered by removing certain nodes 109 from the within the network. In 2016, Goodfellow et al.²⁶, undertook the first study that utilised intracranial EEG 110 (iEEG) recordings, alongside pre- and post-operative imaging, to predict in silico the effects of 111 removing macroscopic regions of the cortex in the emergence of epileptiform activity. Key findings 112 113 of this study were replicated using a bistable dynamic network model in work by Sinha et al.²⁷. Khambhati et al.²⁸ simulated cortical resections in virtual brain networks obtained from 114 electrocorticography, and suggested a *push-pull* control effect resulting from a competition between 115 synchronizing and desynchronizing network regions which influence seizure spread. Jirsa *et al.*²⁹ have 116 117 developed a computational approach to support brain surgery based on non-invasive structural data (the Virtual Epileptic Patient). Lopes et al.³⁰ used iEEG recordings to show that scale-free and rich-118 club functional brain networks have specific nodes that are central for seizure generation and, 119 120 therefore, should be targeted in resective surgery. 121

122 Whilst these approaches have shown promise, it is very important to consider the implications of the 123 assumptions underlying both epilepsy surgery and the models with which predictions of outcome are made. One critical assumption is that the perturbation to the brain as a consequence of the surgery is 124 ever lasting. However, there is no reason to assume that connections between remaining regions of the 125 brain stay static post-surgery. On the contrary, the brain is highly plastic³¹ and evidence of ongoing 126 changes are supported by the clinical observations of declining seizure freedom over time in people 127 who have undergone apparently successful surgery^{6,7}. A further challenge is that we do not know a128 *priori* how best to mathematically characterise brain dynamics that underpin the emergence of seizures 129 within a dynamic network. Recent work³² has demonstrated that predictions of the outcome of surgical 130 strategies may depend on the choice of mathematical model that defines the behaviour of each node 131 within the network. 132

133

Collectively these issues relate to dynamic robustness. By this we mean how do ongoing dynamic factors impact upon the choice of perturbation that we might make. This is an important consideration in the context of epilepsy surgery. For example, there may be multiple routes to achieving apparent seizure freedom, however some may be more dynamically robust than others. In this work we evaluate how network topology influences seizure propensity, and quantify the effects of virtual surgical resection, represented by the removal of network nodes. Finally, the results are extended to larger networks, more in line with measures obtained from clinical data.

142 II. Methods

143

144 A. Dynamic Network Model

145

146 We consider a bistable dynamic network model that can generate both healthy background-like and 147 seizure-like activity at a phenomenological level^{21,22}. Activity within each brain region is described by 148 a modified version of the normal form of the subcritical Hopf bifurcation, with an additional equation 149 to describe slow variations of the "excitability" variable $\lambda^{22,33}$:

151
$$\frac{dz_j}{dt} = z_j(\lambda_j - 1 + i\omega + 2|z_j|^2 - |z_j|^4) + \frac{\beta}{N} \sum_{k=1}^N A_{kj}(z_k - z_j) + \alpha dW_j \quad (1)$$

152
$$\tau \frac{d\lambda_j}{dt} = \lambda_{j0} - \lambda_j - |z_j|^2 \quad (2)$$

153 where j = 1, ..., N represent the network nodes. These coupled stochastic differential equations 154 describe the evolution of complex variables z, where the coupling is linear and proportional to the 155 difference between node states. The real part of the state variables can be thought of as a proxy of the 156 157 electrographic activity of a brain region, for example as measured using EEG. In this framework, network nodes are associated to regions of the brain generating the electrical signal measured by the 158 EEG electrodes. When $\lambda_i \in [0,1]$, there are two distinct dynamical behaviour: low-amplitude noisy 159 activity near the origin (stable fixed point z = 0) and large amplitude, oscillations (stable limit cycle 160

at $|z|^2 = 1 + \sqrt{\lambda}$. These two stable attractors are separated by an unstable limit cycle (located at 161 $|z|^2 = 1 - \sqrt{\lambda}$). At a phenomenological level, the stable fixed point can be thought of as "background-162 like" activity as observed in electrographic recordings, whereas the stable limit cycle corresponds to 163 "seizure-like" activity. For large enough noise, the system will eventually transition into the seizure-164 165 like state, after which the slow variable decreases (past the limit point located at 0) and the system will 166 return back (with time-scale τ) to the background-like state.

167

Consequently, this phenomenological model provides a framework in which one can systematically 168 169 examine how different model components (e.g. noise, network structure, baseline excitability, coupling strength) impact the propensity of seizure-like activity. Full details of model variables and 170 171 parameters are provided in Tables 1 and 2.

172

Variable	Interpretation	Dimension
Z_j	Complex activity variable of node j	2 x N
λ_j	Excitability of node j	Ν
W_{j}	Complex Wiener process	2 x N

Table 1: Model variables.

173 174

Parameter	Interpretation	Typical range	Value
Ν	Number of nodes in the network	3-10	4
ω	Frequency of the stable limit cycle	3-50	20
β	Coupling strength between nodes	0.05-6	-
α	Noise strength	0.005-0.10	0.08
τ	Time-scale of the slow variable λ	5-50	5
λ_{j0}	Baseline level of excitability	€ [0,1]	0.75
Α	Adjacency matrix	1 (connection), 0 (no connection)	-

175

 Table 2: Model parameter values³³.

176

An example of the dynamics observed in a network with 4 nodes is shown in Fig. 1. The phase diagram 177 178 (Fig. 1B) shows that the system spends most of the time near the fixed point z = 0. In this regime the

179 simulated EEG activity $(Re(z_i))$ remains in the background state (low amplitude noisy oscillations on

the panels on the right). Eventually, the trajectory crosses the boundary of the basin of attraction of the 180

181 fixed point (dashed line) and transitions into the seizure-like state. A drop in the excitability variable 182 λ follows (see equation 2) and the system is brought back to the proximity of the fixed point (the

183 background state).184



185 λ Fig. 1: Example of network dynamics for a 4-node network. (A) Specific network structure. (B) Trajectory in phase 187 space for node 1 (other nodes display similar patterns). The direction of the flow is anti-clockwise (see arrows). (C) 188 simulated electrographic (e.g. EEG) activity ($Re(z_j)$) for the four nodes, amplitude of the complex activity variables 189 ($|z_j|^2$), and slow excitability variables (λ_j). Note that all nodes transitioned simultaneously into the seizure-like state 190 (synchronization). All simulations were carried with an Euler-Maruyama scheme with dt = 0.0001. See Table 2 for 191 default values for the model parameters.

For certain classes of coupled bistable systems with noise-induced transitions, it is be possible to analytically examine the behaviours of these systems, for example, derive analytical expressions for the escape time using the Eyring-Kramer equation^{34,35}. These escape times have been shown to correlate with seizure propensity^{22,36}. In general, however, these high-dimensional dynamic network models do not allow for such analytical treatment and numerical simulations can provide insight into how different mechanisms contribute to seizure propensity.

200 B. Brain Network Ictogenicity

199

201

Recently, several works have used the concept of *Brain Network Ictogenicity (BNI)* to estimate the
 propensity of a network to generate what we term seizure-like activity^{36,37}. For example identifying
 optimal resection regions in epilepsy brain surgery^{26,27,30}, to classify focal and generalized epilepsies³⁹,
 and to assess lateralization in focal epilepsy⁴⁰.

206 207 Broadly speaking, BNI can be thought of as the proportion of time that nodes within a network spend in a seizure-like state. The propensity of seizure-like activity critically depends on the interplay 208 209 between a number of model parameters. In particular the coupling strength (β), noise strength (α), the 210 time-constant of the slow variable (τ) , the network topology (for example, whether it is strongly or weakly connected, the presence of cycles) and the baseline excitability (λ_{i0}). For example, if the 211 baseline excitability λ_{j0} is close to 0, low values of noise strength α are unlikely to lead to seizures 212 213 whereas if λ_{i0} is close to 1, the same strength of noise would lead to several seizures. In practice the calculation of BNI can be implemented in several different ways and depends on many factors, 214 215 including the specific dynamical model, the precise definition of what characterizes a seizure in this

system, the details of the state transition, model parameters, and coupling type, amongst others. Despite these many factors, the value of *BNI* calculated using different models is often similar^{30,32}.

An important consideration when calculating *BNI* is to define what constitutes a seizure within the context of the model. For the model we consider, there are two stable attractors, which correspond to a background state and a seizure-like state, and therefore we can use the separatrix as a threshold for whether a node is in the seizure-like state. The details on how such a threshold is defined are often omitted, in spite of the fact that this threshold often has an influence on the absolute values of the *BNI*.

In this study we are primarily interested in the effect of the network structure on seizure propensity, we focus on when seizure-like activity across multiple nodes is driven by the connectivity between them. Consequently, the *BNI* for a given dynamic network structure is quantified by evaluating how long two or more nodes are simultaneously in the seizure-like state (this means that if a single individual node is in the seizure-like state whilst the other N - 1 nodes are in the background state, we do not consider this to be a seizure).

To quantify the *BNI* for a given simulation of the dynamic network model, we start by finding all segments in the simulation where at least two nodes are simultaneously in the high-amplitude seizurelike state $(|z_j|^2 > 0.5)$. The *BNI* is defined as the total sum of the lengths of these segments, scaled by $m/(T_sN)$, where *m* is the number of nodes in the seizure-like state in each segment ($m \ge 2$), T_s is the total simulation time and *N* is the total number of nodes.

Consequently, it holds that $BNI \in [0,1]$, where a value of 0 means there was no synchronised seizurelike activity in the simulation, whereas a value of 1 means that all nodes were in the seizure-like state for the entire simulation. See Fig. 2 for a simple example of how the *BNI* is calculated for a given dynamic network model.



243 244

224

231

237

Fig. 2: The *BNI* calculated for a four-nodes network. (A) directed, unweighted network consisting of four nodes. (B) simulated electrographic recording. This simulation contained one segment for which at least 2 nodes have $|z_j(i)|^2 > 0.5$ (dotted box at approximately 550 seconds). Model simulation with: $\beta = 0.20$, $T_s = 1000$; Euler-Maruyama scheme with dt = 0.0001; initial conditions: $z_j(0) \approx 0$ and $\lambda_j(0) \approx \lambda_{j0}$, for all other default values see Table 2.

Systematic explorations of the key parameters allow one to extend the *BNI* as a high-dimensional integral for a given network structure. Fig. 3 shows the dependence of seizure propensity to the choice of parameters of the dynamic network model. Even though small changes in parameter values seem to lead to smooth, monotonic changes in the *BNI*, this suggests it is in general important to consider the certainty of parameter inference in networks of dynamic models as this could significantly impact the higher-level model outputs of interest.

255

261

263



Fig. 3: Seizure propensity (as quantified by *BNI*) depends on the coupling strength β , baseline excitability λ_{j0} and the slow time-scale τ . The *BNI* landscape computed for a given network structure (A) for different values of β and λ_{j0} . (B) $\tau = 5$; (C) $\tau = 50$. All simulations with total simulation time: T_s = 1000, using an Euler-Maruyama scheme with dt = 0.0001; $\alpha = 0.08$. Initial conditions: $z_j(0) \approx 0$ and $\lambda_j(0) \approx \lambda_{j0}$.

262 C. Perturbations to network structure

To explore the effect of changes to network topology, such as the removal of a node or the addition or removal of an edge, we start with network structures with four nodes. Initially, we only consider network structures that are at least weakly connected, which guarantees there are no disconnected nodes or subgraphs. If a network perturbation renders the network disconnected, the *BNI* of the perturbed network is determined by the connected component with the largest *BNI*.

270 In order to consider all potential types of behaviour for a given network structure, we do not restrict our analysis to a single value of the coupling parameter. The BNI is averaged over a wide range of 271 values for β (see Table 2), covering all from weak to strong coupling relative to noise and excitability. 272 Additionally, in this work we are not concerned with absolute values of the seizure propensity, which 273 can be influenced by the baseline excitability (λ_{i0}) , the timescale of the slow variable (τ) , or the noise 274 (α); but with the difference between the BNI before and after a network is perturbed, either by a node 275 276 removal or by network reconfiguration. Therefore, a consistent choice for these parameters is sufficient 277 to reveal the influence of network perturbations in seizure propensity. For the choices of fixed 278 parameters please see Table 2.

279 280

281 III. Results282

283 To understand the impact on network ictogenicity of virtual resections, and how this is further impacted by continued reorganization of the remaining network, we begin by performing a systematic 284 analysis of networks with four nodes. We first establish the relationship between network structure 285 286 and BNI for the given choice of fixed parameters in Table 2. We use this understanding to measure the change in BNI upon removal of individual nodes within different network structures, focussing on 287 288 cases where the original network has high BNI. This focus is motivated by the potential clinical application, where such networks might be potentially suitable for surgical intervention. The impact 289 of ongoing network reorganisation post virtual resection is evaluated by considering all possible 290 individual edge changes in an exemplar network. We find examples where removal of a node results 291 292 in a network with low BNI – the desired outcome – however, creating or removing individual edges

results in a dramatic increase in *BNI*. Finally, we show how this effect can also manifest in larger networks, more in line with brain networks obtained from clinical data.

295 296

297

A. Network ictogenicity for 4-nodes networks

298 There are 199 non-isomorphic networks with four nodes that are weakly or strongly connected. In Fig. 299 4(A) we present calculations of the BNI where networks are sorted by increasing number of edges and, within each edge group, by decreasing value of BNI. By comparing the BNI values for networks with 300 301 3 or 4 edges, and those with 10, 11 and 12 edges, we observe a tendency for networks to present, on average, decreasing BNI as the number of edges in the network increases. For networks with 4 to 9 302 edges, the proportion of networks with relatively low values of BNI similarly grows with increasing 303 304 number of edges. This behaviour is due to the nature of the coupling between nodes within the network 305 (linear and proportional to the difference between node states), whereby a connection from node A to 306 node B results in node A influencing node B to behave in the same way. Combined with node dynamics being brought back to the background state with time-scale τ following transition to the seizure-like 307 state, this makes network nodes hold themselves more strongly in the background state when there are 308 309 more connections within a network.

310

311 However, it is important to recognise that BNI does not decrease monotonically with increasing number of edges. Rather, the effect of the network topology, and the hierarchy of the network in 312 particular, plays an important role. Interestingly, all edge groups in Fig. 4(A) present a similar pattern 313 314 on how the BNI decreases. Within each group, networks with relatively high BNI are those with a 315 single "driving" node (e.g. a node with no in-connections). An example of such a network is presented in panel N1 of Fig. 4 (6-edges network with highest BNI). In this example, node 2 is not being 316 influenced to remain in the background state by any other nodes, and when it transits to the seizure-317 318 like state, it forces nodes 1, 3 and 4 to the same state, leading to a relatively high seizure propensity. The network in panel N₂ considers a case with two driver nodes (2 and 3) which are connected to nodes 319 1 and 4. Nodes 2 and 3 have a similar influence here as node 2 in network N1. When both nodes transit 320 to the seizure-like state together, they force nodes 1 and 4 to the same state. However, in the case 321 322 where one node is in the seizure-like state and the other remains in the background state, they exert 323 opposite influences upon nodes 1 and 4. This competition leads to intermediate values of BNI for networks with this general structure. Finally, network in panel N3 is strongly connected and all nodes 324 325 tend to hold each other in the background state, resulting in low values of BNI. 326



327 328

Fig. 4: (A) *BNI* for all networks with 4 nodes, sorted first by increasing number of edges (between 3 and 12), then by decreasing *BNI*. Exemplar 6-edges networks are presented for high (N₁), intermediate (N₂) and low (N₃) values of *BNI*.
 Error bars represent variations due to noise.

332333 B. Effects of node removal

Epilepsy surgery aims to reduce seizure propensity through the removal of cortical tissue considered key to generating seizures⁴¹. Within the context of our dynamic network model, we explore this through systematic removal of individual nodes and studying the impact on the level of *BNI* as a result. Nodes identified as being essential to the emergence and/or spreading of seizure-like activity would represent the best candidates for surgical resection. It is important to note on the other hand that some nodes may influence emergent dynamics in such a way as to prevent the spread of seizures, and the removal of such nodes might lead to even more seizures.

342

343 To consider these issues Fig. 5(A) illustrates the distribution of BNI before and after the removal of each node individually for a given four-node network. The diagonal line separates the cases where the 344 345 BNI after node removal is smaller than before (blue region) from the cases where a removal leads to a remaining network with higher BNI (red region). The networks clustered on the left side of the figure 346 have a low BNI and any intervention either leads to a similar or higher BNI. On the opposite side, 347 networks with high BNI are those potential candidates for node removal in order to try to reduce the 348 overall seizure propensity. However, not all networks can lead to lower BNI by node removal. From 349 350 the 58 networks clustered in the region of high BNI before node removal (BNI > 0.055), 37 (63.8%) 351 have at least one node removal that leads to a network with significantly lower ictogenicity (BNI < 0.020). From the 232 possible node removals (58 networks \times 4 nodes), only 45 (19.4%) lead to a 352 significant reduction in BNI. 353

Two exemplar networks with high *BNI* are shown in Fig. 5 (N_1 and N_2). The removal of nodes 1, 3 or 4 in the network in N_1 lead to networks with *BNI* very similar to the complete network. However, the removal of node 2 (a driver node) leads to a significant reduction in *BNI*. From a model perspective, this would represent a suitable candidate for therapeutic resection for controlling seizure activity. Conversely, network N_2 also have a relatively high *BNI*, however in this case no node removal lead to a substantial reduction in *BNI*. Here, node removal is not an efficient alternative to reduce network ictogenicity.

362

363 C. Robustness to connectivity changes 364

A critical question to consider is the impact of ongoing network reorganisation following the removal of a node or nodes within the network. Effectively, this is an issue of robustness of a network with respect to increases in *BNI* when edges are either added or removed. To consider this, we evaluate the effect of all possible configurations involving adding or removing a single edge in the remaining network. In Fig. 6 we present an example where network reconfiguration post-removal of a node has a dramatic influence on the level of *BNI*.

371

The starting network presented in Fig. 6(A) has a relatively high *BNI*. As shown in Fig. 6(B), removing nodes 2, 3 or 4 do not result in a significant change in *BNI*. On the other hand, the removal of node 1, which results in the network presented in panel C of the same figure, significantly reduces *BNI*, suggesting this is a suitable candidate for therapeutic intervention. However, if we add or remove a single edge in the remaining network, which would lead to one of the networks presented in panels D, E and F (all other possible combinations are isomorphic to one of these networks), the *BNI* increases to levels similar to those observed prior to node removal (network in panel A).



Fig. 5: (A) *BNI* before and after all possible node removal (four one-node removal). Minimum *BNI* after node removal is
shown in black, others are shown in light grey. Region in blue (red) indicate a decrease (increase) in BNI after node
removal. (N₁ and N₂) Exemplar networks of high *BNI*, with the respective values of the *BNI* after node removal for all
nodes individually. Dashed lines represent *BNI* before node removal. The dots associated to networks N₁ and N₂ in panel
A are shown in green and yellow, respectively.

386 387

This effect is due to the fact that after node 1 was removed, the remaining network has two "competing drivers", similar to the situation described in Fig. $5(N_2)$. This competing influence results in a lower value of the *BNI*, however this configuration is quite unstable. The addition or removal of any edge breaks up the symmetry between the competing elements and a single driver takes over, bringing the *BNI* up again.



Fig. 6: (A) Exemplar network with 4 nodes. (B) *BNI* for the resulting networks after the removal of each of the 4 nodes
individually (dashed line represents *BNI* before node removal). (C) Resulting network after the removal of node 1 (node
removal that leads to the lowest *BNI*). (D, E and F) Resulting networks after removing or adding one edge in the network
in (C), evidencing a clear increase in the *BNI*.

1 D. Evaluation of lager networks

This effect is not an artefact resulting from small network sizes. In Fig. 7 we find similar effects in a 403 network of 10 nodes: a size more in line with the typical network sizes obtained from scalp, stereo or 404 405 intracranial EEG⁴². The network presented in Fig. 7(A) has a relatively high BNI. The effects of removing all nodes individually are presented in Fig. 7(B), and it suggests that only the removal of 406 node 1 leads to a significant reduction in the BNI. The network resulting from removing node 1 is 407 408 presented in Fig. 7(C). This network is formed by two cycles, one involving nodes 2, 3, 4, 5 and 10, 409 and the other by nodes 6, 7, 8, and 9. The cycles are connected by an edge between nodes 9 and 10. This network presents a relatively low BNI. However, if we probe the BNI stability by adding or 410 411 removing individual edges, Fig. 7(D) shows that for over 10% of the resulting networks the BNI 412 increases significantly, sometimes to values even higher than before the removal of node 1.

413

These findings are a potentially important consideration for pre-surgical planning. A strategy that a priori leads to a substantial reduction in *BNI* can result in a remaining network that is prone to a return to high seizure propensity with only a few connections added or removed.



418 419

426

428

Fig. 7: (A) Exemplar network with 10 nodes. (B) *BNI* for the resulting networks after the removal of each of the 10 nodes individually (dashed line represents *BNI* before node removal). (C) Resulting network after the removal of node 1 (node removal that leads to the lowest *BNI*). (D) *BNI* for all 72 possible networks obtained by removing or adding one edge in the network in (C), sorted by decreasing *BNI* (dashed line represents *BNI* before edge change). Note that 8 networks (>10%) present a significant increase in the *BNI*.

427 IV. Discussion

In this paper we used a canonical dynamic network model to explore seizure propensity in brain networks. We showed that due to the interplay of coupling between brain regions and the excitability within brain regions, a decrease in *BNI* is correlated with an increased number of edges within the network. We further showed that the hierarchy of the network plays a crucial role in the level of *BNI*: the presence of a single driving node leads to high values of *BNI*, competing driver nodes typically result in intermediate levels of ictogenicity, whilst strongly connected networks tend to present very low ictogenicity.

436

437 Building on these observations, we systematically evaluated how removal of network nodes influences the ictogenicity of the remaining network. These so-called virtual resections are effectively an *in silico* 438 proxy for brain surgery, enabling the relative merits of alternative surgical strategies to be evaluated. 439 Of particular importance is the robustness of an intervention to future evolution of the remaining 440 441 network. To investigate this, we systematically studied the impact on BNI of adding or removing edges 442 within a network for which a node had been previously removed. We found networks for which 443 initially high BNI was significantly reduced upon removal of a specific node. However, any alterations 444 to the remaining network led to a return to high levels of BNI, similar to those prior to node removal.

446 A potential limitation of our study is that BNI is agnostic to seizure-frequency: a simulation in which 447 all nodes enter the seizure-like state for 20 seconds has the same BNI as a simulation in which all 448 nodes enter the seizure-like state ten times for 2 seconds each. In addition, identical values of BNI 449 can be achieved through different mechanisms and patterns of activity. However, in contexts where the differentiation between specific seizure patterns are important, the BNI framework described in 450 this work can be extended. For example, Lopes et al.³⁹ have used the average slope of the BNI as a 451 function of the coupling strength (what the authors called the *Ictogenic Spread*) to classify genetic 452 generalized epilepsy versus mesial temporal lobe epilepsy. Woldman et al.43 introduced two 453 454 measures: the onset index and the participation index that incorporate the level of synchronised 455 activity within brain regions and the ability of those brain regions to either drive seizure onset, or to 456 become involved in such activity. Furthermore, these potential limitations are likely to be context 457 dependent. For example, people with epilepsy may place high value on measuring the number of 458 seizures they experience, whilst the total duration of those events is less important. On the other 459 hand, a neurosurgeon planning surgery, will primarily be concerned with how a specific resection 460 will affect a given, baseline, seizure propensity. We finally note that the results of our work are not 461 impacted by these limitations, since we are interested in seizure susceptibility more generally, 462 independent of any specific activity patterns.

463

445

Taking into account the robustness of a perturbed network to subsequent alterations to its connectivity is an important consideration in pre-surgical planning. For example, there may be competing strategies which result in an initial reduction in seizure propensity. However, one is more sensitive to subsequent network alterations than the other. Therefore, an important next step for this research is the application of these theoretical concepts to networks inferred directly from clinical data. This would provide the opportunity to better characterise long-term seizure freedom, given an apparently successful surgical intervention.

472 Acknowledgments

LJ and JRT acknowledge financial support from the EPSRC via grant EP/N014391/1. LJ, WW and JRT acknowledge financial support from Innovate UK via grant TS/R00546X/1. WW acknowledges financial support from the MRC (MR/N01524X/1) and from Epilepsy Research UK (F2002). WW and JRT are co-founders of Neuronostics.

477

480

482

The data that support the findings of this study are available from the corresponding author uponreasonable request.

481 **References**

- 483 1. WHO | Epilepsy. *WHO* (2017).
- 484 2. Banerjee, P. N., Filippi, D. & Allen Hauser, W. The descriptive epidemiology of epilepsy-A
 485 review. *Epilepsy Research* (2009).
- 486 3. Kwan, P. & Brodie, M. J. Early identification of refractory epilepsy. N. Engl. J. Med. (2000).
- 4. Fisher, R., Salanova, V., Witt, T., Worth, R., Henry, T., Gross, R., Oommen, K., Osorio, I.,
 488 Nazzaro, J., Labar, D., Kaplitt, M., Sperling, M., Sandok, E., Neal, J., Handforth, A., Stern, J.,
 489 DeSalles, A., Chung, S., Shetter, A., *et al.* Electrical stimulation of the anterior nucleus of
 490 thalamus for treatment of refractory epilepsy. *Epilepsia* (2010).
- 491 5. Duncan, J. S., Winston, G. P., Koepp, M. J. & Ourselin, S. Brain imaging in the assessment for epilepsy surgery. *Lancet Neurol.* 15, 420–433 (2016).
- 493 6. De Tisi, J., Bell, G. S., Peacock, J. L., McEvoy, A. W., Harkness, W. F., Sander, J. W. &
 494 Duncan, J. S. The long-term outcome of adult epilepsy surgery, patterns of seizure remission,

- 495 and relapse: A cohort study. *Lancet* **378**, 1388–1395 (2011).
- 496 7. Mohan, M., Keller, S., Nicolson, A., Biswas, S., Smith, D., Farah, J. O., Eldridge, P. &
 497 Wieshmann, U. The long-term outcomes of epilepsy surgery. *PLoS One* (2018).
- 498 8. Sheikh, S. R., Kattan, M. W., Steinmetz, M., Singer, M. E., Udeh, B. L. & Jehi, L. Cost
- 499 effectiveness of surgery for drug resistant temporal lobe epilepsy in the US. *Neurology* (2020).
 500 9. Engel, J. Surgery for Seizures. *N. Engl. J. Med.* (1996).
- 501 10. Engel, J. J. The current place of epilepsy surgery. Curr. Opin. Neurol. (2017).
- 502 11. Kramer, M. A. & Cash, S. S. Epilepsy as a Disorder of Cortical Network Organization.
 503 *Neurosci.* 18, 360–372 (2012).
- Richardson, M. P. Large scale brain models of epilepsy: dynamics meets connectomics. J.
 Neurol. Neurosurg. Psychiatry 83, 1238–1248 (2012).
- Van Diessen, E., Diederen, S. J. H., Braun, K. P. J., Jansen, F. E. & Stam, C. J. Functional and structural brain networks in epilepsy: What have we learned? *Epilepsia* (2013).
- 508 14. Geier, C. & Lehnertz, K. Long-term variability of importance of brain regions in evolving
 509 epileptic brain networks. *Chaos* (2017).
- 510 15. Li Hegner, Y., Marquetand, J., Elshahabi, A., Klamer, S., Lerche, H., Braun, C. & Focke, N.
 511 K. Increased Functional MEG Connectivity as a Hallmark of MRI-Negative Focal and
 512 Generalized Epilepsy. *Brain Topogr.* (2018).
- 513 16. van Mierlo, P., Höller, Y., Focke, N. K. & Vulliemoz, S. Network Perspectives on Epilepsy
 514 Using EEG/MEG Source Connectivity . *Frontiers in Neurology* vol. 10 721 (2019).
- Fisher, R. S., Cross, J. H., French, J. A., Higurashi, N., Hirsch, E., Jansen, F. E., Lagae, L.,
 Moshé, S. L., Peltola, J., Roulet Perez, E., Scheffer, I. E. & Zuberi, S. M. Operational
 classification of seizure types by the International League Against Epilepsy: Position Paper of
 the ILAE Commission for Classification and Terminology. *Epilepsia* (2017).
- 519 18. Stam, C. J. Modern network science of neurological disorders. *Nature Reviews Neuroscience* (2014).
- 521 19. Woldman, W. & Terry, J. R. Multilevel Computational Modelling in Epilepsy: Classical
 522 Studies and Recent Advances. in *Validating Neuro-Computational Models of Neurological*523 *and Psychiatric Disorders* (eds. Bhattacharya, B. S. & Chowdhury, F. N.) 161–188 (2015).
- 524 20. Terry, J. R., Benjamin, O. & Richardson, M. P. Seizure generation: The role of nodes and networks. *Epilepsia* 53, (2012).
- 526 21. Kalitzin, S. N., Velis, D. N. & Lopes da Silva, F. H. Stimulation-based anticipation and control of state transitions in the epileptic brain. *Epilepsy Behav.* (2010).
- Benjamin, O., Fitzgerald, T. H., Ashwin, P., Tsaneva-Atanasova, K., Chowdhury, F.,
 Richardson, M. P. & Terry, J. R. A phenomenological model of seizure initiation suggests
 network structure may explain seizure frequency in idiopathic generalised epilepsy. *J. Math. Neurosci.* 2, 1 (2012).
- 532 23. Milton, J. & Jung, P. *Epilepsy as a Dynamic Disease*. (Springer Berlin Heidelberg, 2003).
- 533 24. Moraes, M. F. D., de Castro Medeiros, D., Mourao, F. A. G., Cancado, S. A. V. & Cota, V. R.
 534 Epilepsy as a dynamical system, a most needed paradigm shift in epileptology. *Epilepsy and*535 *Behavior* (2019).
- 536 25. Hutchings, F., Han, C. E., Keller, S. S., Weber, B., Taylor, P. N. & Kaiser, M. Predicting
 537 Surgery Targets in Temporal Lobe Epilepsy through Structural Connectome Based
 538 Simulations. *PLoS Comput. Biol.* (2015).
- 539 26. Goodfellow, M., Rummel, C., Abela, E., Richardson, M. P., Schindler, K. & Terry, J. R.
 540 Estimation of brain network ictogenicity predicts outcome from epilepsy surgery. *Sci. Rep.* 6, 29215 (2016).
- Sinha, N., Dauwels, J., Kaiser, M., Cash, S. S., Westover, M. B., Wang, Y. & Taylor, P. N.
 Predicting neurosurgical outcomes in focal epilepsy patients using computational modelling. *Brain* 140, 319–332 (2016).

- 545 28. Khambhati, A. N., Davis, K. A., Lucas, T. H., Litt, B. & Bassett, D. S. Virtual Cortical
 546 Resection Reveals Push-Pull Network Control Preceding Seizure Evolution. *Neuron* (2016).
- Jirsa, V. K., Proix, T., Perdikis, D., Woodman, M. M., Wang, H., Bernard, C., Bénar, C.,
 Chauvel, P., Bartolomei, F., Bartolomei, F., Guye, M., Gonzalez-Martinez, J. & Chauvel, P.
 The Virtual Epileptic Patient: Individualized whole-brain models of epilepsy spread. *Neuroimage* 145, 377–388 (2017).
- 30. Lopes, M. A., Richardson, M. P., Abela, E., Rummel, C., Schindler, K., Goodfellow, M. &
 Terry, J. R. An optimal strategy for epilepsy surgery: Disruption of the rich-club? *PLoS Comput. Biol.* (2017).
- 554 31. Johnston, M. V. Clinical disorders of brain plasticity. *Brain and Development* (2004).
- Junges, L., Lopes, M. A., Terry, J. R. & Goodfellow, M. The role that choice of model plays
 in predictions for epilepsy surgery. *Sci. Rep.* 9, 7351 (2019).
- 33. Hebbink, J., Meijer, H., Huiskamp, G., van Gils, S. & Leijten, F. Phenomenological network
 models: Lessons for epilepsy surgery. *Epilepsia* 58, e147–e151 (2017).
- 559 34. Neiman, A. Synchronizationlike phenomena in coupled stochastic bistable systems. *Phys. Rev.*560 *E* (1994).
- 35. MacKay, R. S. & Sepulchre, J. A. Multistability in networks of weakly coupled bistable units. *Phys. D Nonlinear Phenom.* (1995).
- 36. Ashwin, P., Creaser, J. & Tsaneva-Atanasova, K. Fast and slow domino regimes in transient network dynamics. *Phys. Rev. E* (2017).
- 565 37. Petkov, G., Goodfellow, M., Richardson, M. P. & Terry, J. R. A critical role for network
 566 structure in seizure onset: A computational modeling approach. *Front. Neurol.* 5, (2014).
- 567 38. Lopes, M. A., Junges, L., Woldman, W., Goodfellow, M. & Terry, J. R. The Role of
 568 Excitability and Network Structure in the Emergence of Focal and Generalized Seizures.
 569 *Front. Neurol.* (2020).
- S70 39. Lopes, M. A., Perani, S., Yaakub, S. N., Richardson, M. P., Goodfellow, M. & Terry, J. R.
 S71 Revealing epilepsy type using a computational analysis of interictal EEG. *Sci. Rep.* (2019).
- 40. Lopes, M. A., Junges, L., Tait, L., Terry, J. R., Abela, E., Richardson, M. P. & Goodfellow,
 M. Computational modelling in source space from scalp EEG to inform presurgical evaluation
 of epilepsy. *Clin. Neurophysiol.* (2020).
- 575 41. Rosenow, F. & Lüders, H. Presurgical evaluation of epilepsy. *Brain* **124**, 1683–1700 (2001).
- 42. Aminoff, M. J. Aminoff's Electrodiagnosis in Clinical Neurology. Aminoff's Electrodiagnosis
 577 in Clinical Neurology (2012).
- Woldman, W., Schmidt, H., Abela, E., Chowdhury, F. A., Pawley, A. D., Jewell, S.,
 Richardson, M. P. & Terry, J. R. Dynamic network properties of the interictal brain determine
 whether seizures appear focal or generalised. *Sci. Rep.* 10, 7043 (2020).
- 581